

1.

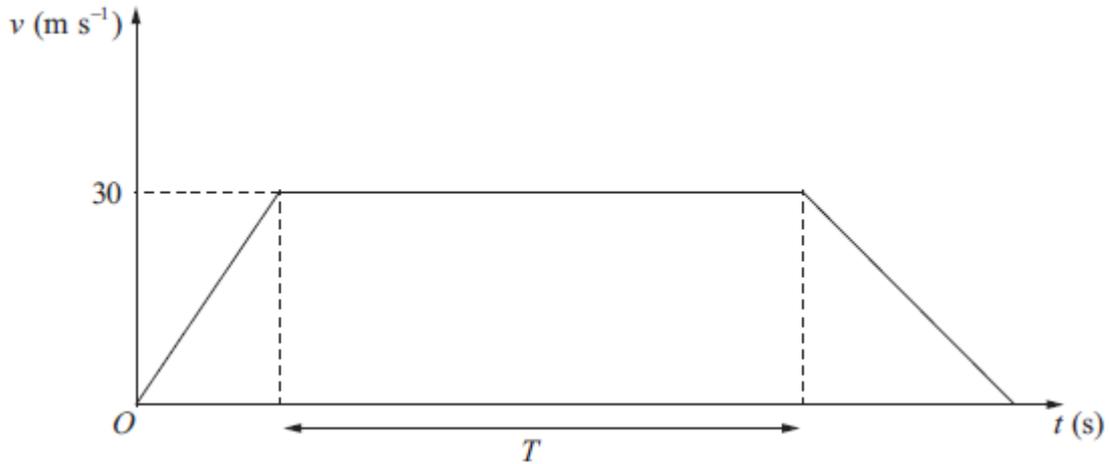


Figure 4

The velocity-time graph in Figure 4 represents the journey of a train P travelling along a straight horizontal track between two stations which are 1.5 km apart. The train P leaves the first station, accelerating uniformly from rest for 300 m until it reaches a speed of 30 m s^{-1} . The train then maintains this speed for T seconds before decelerating uniformly at 1.25 m s^{-2} , coming to rest at the next station.

(a) Find the acceleration of P during the first 300 m of its journey. (2)

(b) Find the value of T . (5)

A second train Q completes the same journey in the same total time. The train leaves the first station, accelerating uniformly from rest until it reaches a speed of $V \text{ m s}^{-1}$ and then immediately decelerates uniformly until it comes to rest at the next station.

(c) Sketch on the diagram above, a velocity-time graph which represents the journey of train Q . (2)

(d) Find the value of V . (6)

(Total 15 marks)

2. A stone is projected vertically upwards from a point A with speed u m s⁻¹. After projection the stone moves freely under gravity until it returns to A . The time between the instant that the stone is projected and the instant that it returns to A is $3\frac{4}{7}$ seconds.

Modelling the stone as a particle,

- (a) show that $u = 17\frac{1}{2}$, (3)
- (b) find the greatest height above A reached by the stone, (2)
- (c) find the length of time for which the stone is at least $6\frac{3}{5}$ m above A . (6)

Total 11 marks)

3. A car accelerates uniformly from rest for 20 seconds. It moves at constant speed v m s⁻¹ for the next 40 seconds and then decelerates uniformly for 10 seconds until it comes to rest.

- (a) For the motion of the car, sketch
- (i) a speed-time graph,
- (ii) an acceleration-time graph. (6)

Given that the total distance moved by the car is 880 m,

- (b) find the value of v . (4)

(Total 10 marks)

4. A cyclist is moving along a straight horizontal road and passes a point A . Five seconds later, at the instant when she is moving with speed 10 m s⁻¹, she passes the point B . She moves with constant acceleration from A to B .

Given that $AB = 40$ m, find

- (a) the acceleration of the cyclist as she moves from A to B , (4)
- (b) the time it takes her to travel from A to the midpoint of AB . (5)

(Total 9 marks)

5. A car moves along a straight horizontal road from a point A to a point B , where $AB = 885$ m. The car accelerates from rest at A to a speed of 15 m s^{-1} at a constant rate $a \text{ m s}^{-2}$.

The time for which the car accelerates is $\frac{1}{3}T$ seconds. The car maintains the speed of 15 m s^{-1} for T seconds. The car then decelerates at a constant rate of 2.5 m s^{-2} stopping at B .

- (a) Find the time for which the car decelerates. (2)
- (b) Sketch a speed-time graph for the motion of the car. (2)
- (c) Find the value of T . (4)
- (d) Find the value of a . (2)
- (e) Sketch an acceleration-time graph for the motion of the car. (3)

(Total 13 marks)

6. A train travels along a straight horizontal track between two stations, A and B . The train starts from rest at A and moves with constant acceleration 0.5 m s^{-2} until it reaches a speed of $V \text{ m s}^{-1}$, ($V < 50$). The train then travels at this constant speed before it moves with constant deceleration 0.25 m s^{-2} until it comes to rest at B .

- (a) Sketch a speed-time graph for the motion of the train between the two stations A and B . (2)

The total time for the journey from A to B is 5 minutes.

- (b) Find, in terms of V , the length of time, in seconds, for which the train is
- (i) accelerating,
- (ii) decelerating,
- (iii) moving with constant speed. (5)

Given that the distance between the two stations A and B is 6.3 km,

- (c) find the value of V . (6)

(Total 13 marks)

7. A particle P is projected vertically upwards from a point A with speed $u \text{ m s}^{-1}$. The point A is 17.5 m above horizontal ground. The particle P moves freely under gravity until it reaches the ground with speed 28 m s^{-1} .

(a) Show that $u = 21$.

(3)

At time t seconds after projection, P is 19 m above A .

(b) Find the possible values of t .

(5)

The ground is soft and, after P reaches the ground, P sinks vertically downwards into the ground before coming to rest. The mass of P is 4 kg and the ground is assumed to exert a constant resistive force of magnitude 5000 N on P .

(c) Find the vertical distance that P sinks into the ground before coming to rest.

(4)

(Total 12 marks)

8.



Figure 3

Two particles P and Q , of mass 0.3 kg and 0.5 kg respectively, are joined by a light horizontal rod. The system of the particles and the rod is at rest on a horizontal plane.

At time $t = 0$, a constant force \mathbf{F} of magnitude 4 N is applied to Q in the direction PQ , as shown in Figure 3. The system moves under the action of this force until $t = 6$ s. During the motion, the resistance to the motion of P has constant magnitude 1 N and the resistance to the motion of Q has constant magnitude 2 N.

Find

- (a) the acceleration of the particles as the system moves under the action of \mathbf{F} , (3)
- (b) the speed of the particles at $t = 6$ s, (2)
- (c) the tension in the rod as the system moves under the action of \mathbf{F} . (3)

At $t = 6$ s, \mathbf{F} is removed and the system decelerates to rest. The resistances to motion are unchanged. Find

- (d) the distance moved by P as the system decelerates, (4)
- (e) the thrust in the rod as the system decelerates. (3)

(Total 15 marks)

TOTAL FOR PAPER: 98 MARKS